#### NOTE:

- 1. Answer question 1 and any FOUR from questions 2 to 7.
- 2. Parts of the same question should be answered together and in the same sequence.

## Time: 3 Hours

#### Total Marks: 100

## 1.

- a) Write a recursive function to count the number of nodes in a binary tree.
- b) Constructor declarations are very much like method declarations. However, some restrictions on constructors should be applied. Explain those restrictions. Write the general syntax of constructor.
- c) What do you mean by complexity of an algorithm? Explain the meaning of worst case analysis and best case analysis in brief.
- d) How many key comparisons and assignments, an insertion sort makes in its worst case?
- e) Define data type and abstract data type. Comment upon the significance of both.
- f) Prove the hypothesis that "A tree having 'm' nodes has exactly (m–1) edges or branches".
- g) Can a Queue be represented by circular linked list with only one pointer pointing to the tail of the queue? Substantiate your answer using an example.

(7x4)

## 2.

- a) Two linked lists contain information of the same type in ascending order. Write a module to merge them to a single sorted linked list.
- b) Given a set of input representing the nodes of a binary tree, write a non recursive algorithm that must be able to output the Pre-order and In-order Traversal.
- c) Reverse the order of elements on a stack S
  - i) using two additional stacks.
  - ii) using one additional queue.

#### (5+8+5)

# 3.

- a) What is a Binary Search Tree (BST)? Make a BST for the following sequence of numbers. 45, 36, 76, 23, 89, 115, 98, 39, 41, 56, 69, 48
  - Write Pre-order, In-order and Post-Order Traversal.
- b) Explain how to implement two stacks in one array A[1..n] in such a way that neither stack overflows unless the total number of elements in both stacks together is n. The PUSH and POP operations should run in O(1) time.
- c) Consider the following specification of a graph G
  - $V(G) = \{1,2,3,4\}$
  - $E(G) = \{(1,2), (1,3), (3,3), (3,4), (4,1)\}$
  - i) Draw an undirected graph.
  - ii) Draw its adjacency matrix.

(9+4+5)

- **4.** a)
- How do you rotate a Binary Tree? Explain right and left rotations with the help of an example.

b) Show the result of running BFS and DFS on the directed graph given below using vertex 3 as source. Show the status of the data structure used at each stage.



5.

- a) Why do we use asymptotic notation in the study of algorithm? Describe commonly used asymptotic notations and give their significance.
- b) Write an algorithm to insert an element to a max-heap that is represented sequentially
- c) In java classes, constructors, methods and fields are regulated using access modifiers. What is access modifier and explain various access modifiers available in java.

(7+5+6)

(9+9)

- 6.
- a) Construct a binary tree whose nodes in in-order and preorder are given as follows: In-order : 10, 15, 17, 18, 20, 25, 30, 35, 38, 40, 50 Preorder: 20, 15, 10, 18, 17, 30, 25, 40, 35, 38, 50
- b) Compare and contrast following sorting techniques with respect to memory space and computing time.
  Insertion Sort, Heap Sort, Merge Sort, Quick Sort.

(9+9)

- 7. Write short notes on **any three** of the following:
- a) B Tree
- b) Merge Sort
- c) Threaded Binary Tree
- d) Height Balance Tree (AVL Tree)

(3x6)