No. of Printed Pages: 11

Sl. No.

B2.1-R5: COMPUTER BASED STATISTICAL AND NUMERICAL METHODS

NOTE:

- 1. Answer question 1 and any FOUR questions from 2 to 7.
- 2. Parts of the same question should be answered together and in the same sequence.
- 3. Only Non-programmable and Non-storage type Scientific Calculator is allowed.

Total Time: 3 Hours Total Marks: 100

- 1. (a) The cumulative distribution function, F(x) is given as F(x) = 0 if x < 0, = (x+1)/2 if $0 \le x < 1$, and = 1 if $1 \le x$. Find P(X = 0)
 - (b) Find the LU decomposition of the matrix:

$$A = \begin{pmatrix} 2 & 7 & 5 \\ 6 & 20 & 10 \\ 4 & 3 & 0 \end{pmatrix}$$

- (c) If A and B are mutually exclusive events such that $P(A) = \frac{1}{4}$, and $P(B) = \frac{3}{5}$, find $P(A^c \cap B^c)$.
- (d) A random variable X has mean, m=10, a variance, $\sigma^2=4$ and an unknown probability distribution. Find the value of k such that $P[|X-10|>=k] \le 0.04$
- (e) Approximate the value of the integral

$$I = \int_{0}^{1} 1/(x^2 + 1) dx$$

Using Simpson's rule

- (f) A sample of 900 members is found to have a mean of 3.4 cm. Can it be reasonably regarded as a sample from a large population with mean 3.25 cm and standard deviation 2.61 cm?
- (g) The joint probability distribution of X and Y is given by f(x, y) = (2x + y)/27, x = 0, 1, 2; y = 0, 1, 2Find the marginal distributions of X and Y. (7x4)
- 2. (a) Add a = 7.654321 and b = 9.12345 in a 5-digit decimal system. Also, find the relative total error, and relative round-off error.
 - (b) Compute an approximate real root of $f(x) = e^x 3x \sin x$, using the Newton-Raphson method correct upto 4 decimal places. (6+12)

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- 3. (a) A multiple-choice test paper contains 50 questions; for each question three answers are given, one of which is correct. The two incorrect answers to any question are designed to be plausible, so that an ignorant candidate could be expected to pick an answer quite at random. If the examination is marked simply by giving one mark per correct answer, what should the pass mark be if the probability that a completely ignorant candidate passes is to be approximately 1%?
 - (b) (i) Prove that a Poisson distribution has equal mean and variance.
 - (ii) A Company produces batteries in a packet of 10. The probability of a battery to be defective is 0.2 %. Find the number of batteries having two defective batteries in a consignment of 10,000 packets. (8+5+5)
- 4. (a) A research was done to find whether women have a greater variation in attitude on voting issues than man. Two independent samples of 31 men and 41 women were taken and the sample variations were found to be 80 for men and 120 for women. Test whether the difference in attitude toward voting issues is significant at 5% level of significance?
 - (b) The number of Car accidents per week in Gurgaon was as follows:

Week:	1	2	3	4	5	6	7	8	9	10
No. of Accidents :	12	8	20	2	14	10	15	6	9	4

Are these frequencies in agreement with the belief that car accident conditions were the same during this 10-week period? (8+10)

- 5. (a) Use the formula for $f'(x_0)$ with error of O(h) to compute the derivative of $f(x) = 1 + x + x^2$ at $x_0 = 1$ taking h = 1, 0.1, 0.01 and 0.001.
 - (b) Perform three iterations of Gauss-Seidel method to solve the system of equations AX = B for the given coefficient matrix and right hand side vector, starting with the initial vector

$$x^{(0)} = (0, 0, 0)$$
and
 $4 \quad 1 \quad 1$

$$A = 1 5 2$$
, and $B = -6$
1 2 3 -4

6. (a) In a study of a new method of teaching arithmetic, claimed to improve on conventional techniques, 400 children were divided at random into two groups A and B, of sizes 250 and 150 respectively. Those in group B were taught using the experimental method, while those in group A were taught by conventional methods. After completion of the course all the pupils were given the same test paper, and the group scores were as follows.

Group A: mean 67.8, variance 60.4,

Group B: mean 70.2, variance 55.6.

Is there any evidence that method B is effective? State O carefully your null hypothesis, alternative hypothesis and conclusion.

(b) Two random samples of sizes 9 and 8, drawn from two normal populations, are characterized as follows;

Population	Sum of squares of deviations from their respective means
I	160
II	91

Can they be regarded as drawn from the two normal populations with same variance ?

$$(F_{0.05} \text{ for 8 and 7 d.f.} = 3.73)$$
 (10+8)

7. (a) The HR of a company collects the following data on 7 persons referring to year of service and their monthly income for the purpose of fixing the monthly income of a person:

Find the regression equation of income on years of service. What initial start would the HR recommend for a person having 13 years of service?

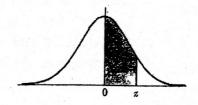
(b) Eight school children, chosen at random from the first year of a large school, were given, without prior warning, a mathematical task, and the time taken (in minutes) by each child to complete the task was recorded. The following day the children were instructed how to perform such tasks efficiently, and a week later they were tested again on a similar task. Once again, the time taken to complete the task was recorded for each child and the results were as follows.

		Time t	aken (1	ninutes	s)			
Child	1	2	3	4	5	6	7	8
Before instruction	26	20	17	21	23	24	21	18
After instruction	19	14	13	16	19	18	16	17

Find a 90% confidence interval for the mean time taken by first year children (i) before instruction, and (ii) after instruction, assuming that times are normally distributed. (8+10)

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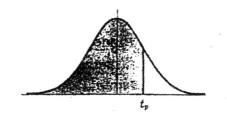
Areas
Under the
Standard
Normal Curve
from 0 to z



z	0	1	2	3	4	5	6	7	8	9
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.035
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.075
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.114
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.151
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.187
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.222
0.6	.2258	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.254
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.285
0.8	.2881	.2910	.2939	.2967	.2996	.3023	.3051	.3078	.3106	.313
0.9	.3159	.3186	-3212	.3238	.3264	.3289	.3315	.3340	.3365	.338
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	3599	.362
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.383
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.401
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.417
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.431
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.444
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.454
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.463
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.470
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.476
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.481
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.485
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.489
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.491
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.493
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.495
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.496
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.497
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.498
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.498
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.499
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.499
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.499
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.499
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.499
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.499
3.6	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.499
3.7	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
3.8	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
3.9	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.500

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Percentile Values (t_p) for Student's t Distribution with ν Degrees of Freedom (shaded area = p)

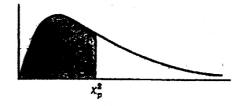


,	t.995	t.99	t.975	t.85	t.00	t.so	t.75	t.70	t.60	t.ss
1	63.66	31.82	12.71	6.31	3.08	1.376	1.000	.727	.325	.158
2	9.92	6.96	4.30	2.92	1.89	1.061	.816	.617	.289	.142
3	5.84	4.54	3.18	2.35	1.64	.978	.765	.584	.277	.137
4	4.60	3.75	2.78	2.13	1.53	.941	.741	.569	.271	.134
5	4.03	3.36	2.57	2.02	1.48	.920	.727	.559	.267	.132
6	3.71	3.14	2.45	1.94	1.44	.906	.718	.553	.265	.131
7	3.50	3.00	2.36	1.90	1.42	.896	.711	.549	.263	.130
8	3.36	2.90	2.31	1.86	1.40	.889	.706	.546	.262	.130
9	3.25	2.82	2.26	1.83	1.38	.883	.703	.543	.261	.129
10	3.17	2.76	2.2 3	1.81	1.37	.879	.700	.542	.260	.129
11	3.11	2.72	2.20	1.80	1.36	.876	.697	.540	.260	.129
12	3.06	2.68	2.18	1.78	1.36	.873	.695	.539	.259	.128
13	3.01	2.65	2.16	1.77	1.35	.870	.694	.538	.259	.128
14	2.98	2.62	2.14	1.76	1.34	.868	.692	.537	.258	.128
15	2.95	2.60	2.13	1.75	1.34	.866	.691	.536	.258	.128
16	2.92	2.58	2.12	1.75	1.34	.865	.690	.535	.258	.128
17	2.90	2.57	2.11	1.74	1.33	.863	.689	.534	.257	.128
18	2.88	2.55	2.10	1.73	1.33	.862	.688	.534	.257	.127
19	2.86	2.54	2.09	1.73	1.33	.861	.688	.533	.257	.127
20	2.84	2.53	2.09	1.72	1.32	.860	.687	.533	.257	.127
21	2.83	2.52	2.08	1.72	1.32	.859	.686	.532	.257	.127
22	2.82	2.51	2.07	1.72	1.32	.858	.686	.532	.256	.127
23	2.81	2.50	2.07	1.71	1.32	.858	.685	.532	.256	.127
24	2.80	2.49	2.06	1.71	1.32	.857	.685	.531	.256	.127
25	2.79	2.48	2.06	1.71	1.32	.856	.684	.531	.256	.127
26	2.78	2.48	2.06	1.71	1.32	.856	.684	.531	.256	.127
27.	2.77	2.47	2.05	1.70	1.31	.855	.684	.531	.256	.127
28	2.76	2.47	2.05	1.70	1.31	.855	.683	.530	.256	.127
29	2.76	2.46	2.04	1.70	1.31	.854	.683	.530	.256	.127
30	2.7 5	2.46	2.04	1.70	1.31	.854	.683	.530	.256	.127
40	2.70	2.42	2.02	1.68	1.30	.851	.681	.529	.255	.126
60	2.66	2.39	2.00	1.67	1.30	.848	.679	.527	.254	.126
120	2.62	2.36	1.98	1.66	1.29	.845	.677	.526	.254	.126
∞ ∞	2.58	2.33	1.96	1.645	1.28	.842	.674	.524	.253	.126

Source: R. A. Fisher and F. Yates, Statistical Tables for Biological, Agricultural and Medical Research (5th edition), Table III, Oliver and Boyd Ltd., Edinburgh, by permission of the authors and publishers.

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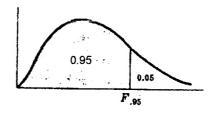
Percentile Values (χ_p^2) for the Chi-Square Distribution with ν Degrees of Freedom (shaded area = p)



Þ	χ ² _{.995}	χ ² .99	X.975	X.95	χ ² _{.90}	X.75	x.50	X2.23	X2.10	x 2 .05	X2.025	X,01	X.005
1	7.88	6.63	5.02	3.84	2.71	1.32	.455	.102	.0158	.0039	.0010	.0002	.0000
2	10.6	9.21	7.38	5.99	4.61	2.77	1.39	.575	.211	.103	.0506	.0201	.0100
3	12.8	11.3	9.35	7.81	6.25	4.11	2.37	1.21	.584	.352	.216	.115	.072
4	14.9	13.3	11.1	9.49	7.78	5.39	3.36	1.92	1.06	.711	.484	.297	.207
5	16.7	15.1	12.8	11.1	9.24	6.63	4.35	2.67	1.61	1.15	.831	.554	.412
6	18.5	16.8	14.4	12.6	10.6	7.84	5.35	3.45	2.20	1.64	1.24	.872	.676
7	20.3	18.5	16.0	14.1	12.0	9.04	6.35	4.25	2.83	2.17	1.69	1.24	.989
8	22.0	20.1	17.5	15.5	13.4	10.2	7.34	5.07	3.49	2.73	2.18	1.65	1.34
9	23.6	21.7	19.0	16.9	14.7	11.4	8:34	5.90	4.17	3.33	2.70	2.09	1.73
10	25.2	23.2	20.5	18.3	16.0	12.5	9.34	6.74	4.87	3.94	3.25	2.56	2.16
11	26.8	24.7	21,9	19.7	17.3	13.7	10.3	7.58	5.58	4.57	3.82	8.05	2.60
12	28.3	26.2	23.3	21.0	18.5	14.8	11.3	8.44	6.30	5.23	4.40	8.57	3.07
13	29.8	27.7	24.7	22.4	19.8	16.0	12. 3	9.30	7.04	5.8 9	5.01	4.11	3.57
14	31.3	29.1	26.1	23.7	21.1	17.1	13.3	10.2	7.79	6.57	5.63	4.66	4.07
15	32.8	30.6	27.5	25.0	22.3	18.2	14.3	11.0	8.55	7.26	6.26	5.23	4.60
16	34.3	32.0	28.8	26.3	23.5	19.4	15.3	11.9	9.31	7.96	6.91	5.81	5.14
17	35.7	33.4	30.2	27.6	24.8	20.5	16.3	12.8	10.1	8.67	7.56	6.41	5.70
18	37.2	34.8	31.5	28.9	26.0	21.6	17.3	13.7	10.9	9.39	8.23	7.01	6.26
19	38.6	36.2	32.9	30.1	27.2	22.7	18.3	14.6	11.7	10.1	8.91	7.63	6.84
20	40.0	37.6	34.2	81.4	28.4	23.8	19.3	15.5	12.4	10.9	9.59	8.26	7.43
21	41.4	38.9	35.5	32.7	29.6	24.9	20.3	16.3	13.2	11.6	10.3	8.90	8.03
22	42.8	40.3	36.8	33.9	80.8	26.0	21.3	17.2	14.0	12.3	11.0	9.54	8.64
.23	44.2	41.6	38.1	35.2	32.0	27.1	22.3	18.1	14.8	13.1	11.7	10.2	9,26
24	45.6	43.0	89.4	36.4	33.2	28.2	23.3	19.0	15.7	13.8	12.4	10.9	9.89
25	46.9	44.3	40.6	37.7	34.4	29.3	24.3	19.9	16.5	14.6	13.1	11.5	10.5
26	48.3	45.6	41.9	38.9	35.6	80.4	25.3	20.8	17.3	15.4	13.8 ·	12.2	11.2
27	49.6	47.0	43.2	40.1	36.7	31.5	26.3	21.7	18.1	16.2	14.6	12.9 .	11.8
28	51.0	48.3	44.5	41.3	37.9	32.6	27.8	22.7	18.9	16.9	15.3	13.6	12.5
29	52.3	49.6	45.7	42.6	39.1	33.7	28.3	23.6	19.8	17.7	16.0	14.3	13.1
80	53.7	50.9	47.0	43.8	40.3	34.8	29.3	24.5	20.6	18.5	16.B	15.0	13.8
40	66.8	63.7	59.3	55.8	51.8	45.6	39.3	83.7					20.7
50	79.5	76.2	71.4	67.5	63.2	56.3	49.3	42.9					28.0
60	92.0	88.4	83.3	79.1	74.4	67.0	59.8	52. 3	46.5				85.5
70	104.2	100.4	95.0	90.5	85.5	77.6	69.3	61.7	55.3	51.7	48.8	45.4	43.3
80	116.3	112.3	106.6	101.9	96.6	88.1	79.3	71.1					51.2
90	128.3	124.1	118.1	113.1	107.6	98.6	89.3	80.6					59.2
100	140.2	135.8	129.6	124.3	118.5	109.1	99.3	90.1					67.3

Source: Catherine M. Thompson, Table of percentage points of the χ^2 distribution, Biometrika, Vol. 32 (1941), by permission of the author and publisher.

95th Percentile Values for the F Distribution (v_1 degrees of freedom in numerator) (v_2 degrees of freedom in denominator)

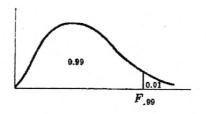


12	1	2	8	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	20
1	161	200	216	225	230	234	237	239	241	242	244	246	248	249	250	251	252	253	254
2	18.5	19.0	19.2	19.2	19.3	19.3	19.4	19.4	19.4	19.4	19.4	19.4	19.4	19.5	19.5	19.5	19.5	19.5	19.5
3	10.1	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.64	8.62	8.59	8.57	8.55	8.53
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.69	5.66	5.63
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46	4.43	4.40	4.37
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.84	3.81	3.77	3.74	3.70	3.67
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.41	3.38	3.34	3.30	3.27	3.23
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.22	3.15	3.12	3.08	3.04	3.01	2.97	2.93
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.90	2.86	2.83	2.79	2.75	2.71
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07		2.98	2.91	2.85		2.74	2.70	2.66	2.62	2.58	2.54
11	4.84	3.98	3.59	3.36	3.20	8.09	3.01	2.95		2.85		2.72		2.61	2.57	2.53	2.49	2.45	2.40
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85		2.75		2.62	2.54	2.51	2.47	2.43	2.38	2.34	2.30
13	4.67	3.81	3.41	3.18	3.03	2.92	2.831			2.67		2.53	2.46	2.42	2.38	2.34		2.25	2.21
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70		2.60		2.46	2.39	2.35	2.31	2.27	2.22		2.13
15	4.54	3 68	3.29	3.06	2.90	2.79	2.71	2.64			2.48	2.40	2.33	2.29	2.25	2.20		2.11	2.07
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66		2.54		2.42	2.35	2.28	2.24		2.15	2.11		2.01
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55		2.45	2.38	2.31		2.19	2.15	2.10	2.06		1.96
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.27	-	2.15	2.11	2.06	2.02		1.92
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48		2.38		2.23	2.16		2.07	2.03	1.98		1.88
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45		2.35	2.28	2.20		2.08	2.04	1.99	1.95		1.84
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42		2.32	2.25	2.18	2.10		2.01	1.96	1.92		1.81
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40		2.30	2.23	2.15	2.07		1.98	1.94	1.89		1.78
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37		2.27		2.13	2.05		1.96	1.91		1.81	1.76
24 25	4.26 4.24	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11		1.98	1.94	1.89	1.84		1.78
26 26	4.23	3.39 3.37	2.99 2.98	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.09		1.96	1.92	1.87	1.82		1.71 1.69
27	4.21	3.35	2.96	2.74 2.73	2.59	2.47	2.39	2.32	2.27	2.22	2.15	2.07		1.95	1.90 1.88	1.85 1.84	1.79	1	1.67
28	4.20	3.34	2.95	2.71	2.57	2.46	2.37	2.31	2.25 2.24	2.20	2.13	2.06		1.93	1.87		1.77		1.65
29	4.18	3.33	2.93	2.71	2.56 2.55	2.45 2.43	2.36	2.29 2.28	2.24	2.19 2.18	2.12 2.10	2.04 2.03	1.96 1.94	1.91 1.90	1.85	1.82 1.81	1.75		1.64
30	4.17	3.32	2.92	2.69	2.53	2.43	2.33	2.28	2.22	2.16	2.10	2.03		1.89	1.84	1.79	1.74		1.62
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.92		1.79	1.74	1.69	1.64		1.51
60	4.00	3.15	2.76	2.53	2.37	2.25	2.23	2.10	2.04	1.99	1.92	1.84		1.70	1.65	1.59	1.53		1.39
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96	1.91	1.83	1.75		1.61	1.55	1.50	1.43		1.25
ec	3.84	3.00	2.60	2.37	2.21	2.10	2.01		1.88	1.83	1.75	1.67		1.52	1.46	1.39	1.32		1.00
	0.01	3.00	2.00	2,01	4.61	2.10	<i>ω.</i> ∪1	1.74	1,00	1.00	1.10	1,01	1.01	1.02	1.20	1.00	1.02	1.20	

Source: E. S. Pearson and H. O. Hartley, Biometrika Tables for Statisticians, Vol. 2 (1972), Table 5, page 178, by permission.

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99^{th} Percentile Values for the *F* Distribution (v_1 degrees of freedom in numerator) (v_2 degrees of freedom in denominator)



P1	Т.		Τ.		Γ.	Γ.	Τ_	Τ_	T	T	П	T	T	T	T	Т	Т	Γ	
P2	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	80
1	4052	5000	5403	5625	5764	5859	5928	5981	6023	6056	6106	6157	6209	6235	6261	6287	6313	6339	6366
2	98.5	99.0	99.2	99.2	99.3	99.3	99.4	99.4	99.4	99.4	99.4	99.4	99.4	99.5	99.5	99.5	99.5	99.5	99.5
3	34.1	30.8	29.5	28.7	28.2	27.9	27.7	27.5	27.3	27.2	27.1	26.9	26.7	26.6	26.5	26.4	26.3	26.2	26.1
4	21.2	18.0	16.7	16.0	15.5	15.2	15.0	14.8	14.7	14.5	14.4	14.2	14.0	13.9	13.8	13.7	13.7	13.6	13.5
5	16.3	13.3	12.1	11.4	11.0	10.7	10.5	10.3	10.2	10.1	9.89	9.72	9.55	9.47	9.38	9.29	9.20	9.11	9.02
. 6	13.7	10.9	9.78	9.15	8.75	8.47	8.26	8.10	7.98	7.87	7.72	7.56	7.40	7.31	7.23	7.14	7.06	6.97	6.88
7	12.2	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72	6.62	6.47	6.31	6.16	6.07	5.99	5.91	5.82	5.74	5.65
8	11.3	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91	5.81	5.67	5.52	5.36	5.28	5.20	5.12	5.03	4.95	4.86
9	10.6	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35	5.26	5.11	4.96	4.81	4.73	4.65	4.57	4.48	4.40	4.31
10	10.0	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94	4.85	4.71	4.56	4.41	4.33	4.25	4.17	4.08	4.00	3.91
11	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63	4.54	4.40	4.25	4.10	4.02	3.94	3.86	3.78	3.69	3.60
12	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.39	4.30	4.16	4.01	3.86	3.78	3.70	3.62	3.54	3.45	3.36
13	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19	4.10	3.96	3.82	3.66	3.59	3.51	3.43	3.34	3.25	3.17
14	8.86	6.51	5.56	5.04	4.70	4.46	4.28	4.14	4.03	3.94	3,80	3.66	3.51	3.43	3.35	3.27	3.18	3.09	3.00
15	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89	3.80	3.67	3.52	3.37	3.29	3.21	3.13	3.05	2.96	2.87
16	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78	3.69	3.55	3.41	3.26	3.18	3.10	3.02	2.93	2.84	2.75
17 18	8.40	6.11	5.19	4.67	4.34	4.10	3.93	3.79	3.68	3.59	3.46	3.31	3.16	3.08	3.00	2.92	2.83	2.75	2.65
19	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60	3.51	3.37	3.23	3.08	3.00	2.92	2.84	2.75	2.66	2.57
20	8.10	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52	3.43	3.30	3.15	3.00	2.92	2.84	2.76	2.67	2.58	2.49
21	8.02	5.78	4.87	4.43	4.10	3.81	3.70	3.56	3.46	3.37	3.23	3.09	2.94	2.86	2.78 2.72	2.69	2.61 2.55	2.52	2.42
22	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.40	3.26	3.12	2.98	2.83	2.75	2.67	2.54	2.50	2.40	2.31
23	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30	3.21	3.07	2.93	2.78	2.70	2.62	2.54	2.45	2.35	2.26
24	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	3.17	3.03	2.89	2.74	2.66	2.58	2.49	2.40	2.31	2.21
25	7.77	5.57	4.68	4.18	3.86	3.63	3.46	3.32	3.22		2.99	2.85	2.70	2.62	2.54	2.45	2.36	2.27	2.17
26	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18		2.96	2.82	2.66	2.58	2.50	2.42	2.33	2.23	2.13
27		5.49	4.60	4:11	3.78	3.56	3.39	3.26			2.93	2.78	2.63	2.55	2.47	2.38	2.29	2.20	2.10
28		5.45	4.57	4.07	3.75	3.53		3.23	- 1		2.90	2.75	2.60	2.52	2.44	2.35	2.26	2.17	2.06
29		5.42	4.54		3.73	3.50			7		2.87	2.73	2.57	2.49	2.41	2.33	2.23	2.14	2.03
30		5.39	4.51		3.70	3.47					2.84	2.70	2.55	2.47	2.39	2.30	2.21	2.11	2.01
40	7.31	5.18	4.31			3.29					2.66	2.52	2,37	2.29	2.20	2.11	2.02	1.92	1.80
60	7.08	4.98	4.13			3.12	1			1		2.35	- 1	2.12	2.03			1.73	1.60
120	6.85	4.79	3.95	3.48	3.17	2.96	- 1			2.47	2.34	2.19	2.03	1.95	1.86	1.76	1.66	1.53	1.38
so	6.63	4.61	3.78	3.32	3.02	2.80	- 1		- 1	- 1		2.04		1.79	1.70	1.59		1	1.00
						<u> </u>													

Source: E. S. Pearson and H. O. Hartley, Biometrika Tables for Statisticians, Vol. 2 (1972), Table 5, page 180, by permission.

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Values of e⁻

(0<1<1)

~	0		83	က	4	2	9	7	0 0	6
0.0	1.0000	.0066	.9802	.9704	9096	.9512	.9418	.9324	.9231	.9139
0.1	.9048	8928	8869	.8781	.8694	.8607	.8521	.8437	.8353	.8270
0.2	.8187	8106	.8025	7945	.7866	.7788	.7711	.7634	.7558	.7483
0.3	.7408	.7334	.7261	.7189	.7118	.7047	.6977	.6907	.6839	.6771
1.0	.6703	.6636	.6570	.6505	.6440	.6376	.6313	.6250	.6188	.6126
0.5	.6065	.6005	5945	.5886	5827	.5770	.5712	.5655	.5599	.5543
9.0	5488	.5434	.5379	.5326	.5273	.5220	5169	.5117	.5066	.5016
0.7	.4966	.4916	.4868	.4819	.4771	.4724	.4677	.4630	.4584	.4538
8.0	.4493	4449	.4404	,4360	.4317	.4274	.4232	.4190	.4148	.4107
6.0	.4066	.4025	3985	.3946	.3906	.3867	.3829	.3791	.3753	.3716

$$(\lambda = 1, 2, 3, ..., 10)$$

~	1	2	က	-4	5	·	7	œ	6	10
6-1.	.36788	.13534	.04979	.01832	.006738	.002479	.000912	.000335	.000123	.000045

Note: To obtain values of $e^{-\lambda}$ for other values of λ , use the laws of exponents. Example: $e^{-3.48} = (e^{-3.00})(e^{-0.44}) = (0.04979)(0.6188) = 0.03081$.

Table 7. Critical Values of the Kolmogorov-Smirnov One Sample TestStatistics This table gives the values of $D_{n,a}^+$ and $D_{n,a}$ for which $\alpha \ge P\{D_n^+ > D_{n,a}^+\}$ and $\alpha > P\{D_n^- > D_{n,a}^-\}$ for some selected values of n and a.

$\frac{n.\alpha^{\prime}}{n}$	4 4										
One-Sid											
$\alpha =$.10	.05	.025	.01	.005	$\alpha =$.10	.05	.025	.01	.005
Two-Si	ded Te	st:									
α=	.20	.10	.05	.02	.01	$\alpha =$.20	.10	.05	.02	.01
n = 1	.900	.950	.975	.990	.995	n = 21	.226	.259	.287	.321	.344
2	.684	.776	.842	.900	.929	22	.221	.253	.281	.314	.337
3	.565	.636	.708	.785	.829	23	.216	.247	.275	.307	.330
4	.493	.565	.624	.689	.734	24	.212	.242	.269	.301	.323
5	.447	.509	.563	.627	.669	25	.208	.238	.264	.295	.317
6	.410	.468	.519	.577	.617	26	.204	.233	.259	.290	.311
7	.381	.436	.483	.538	.576	27	.200	.229	.254	.284	.305
8	.358	.410	.454	.507	.542	28	.197	.225	.250	.279	.300
9	.339	.387	.430	.480	.513	29	.193	.221	.246	.275	.295
10	.323	.369	.409	.457	.489	30	.190	.218	.242	.270	.290
11	.308	.352	.391	.437	.468	31	.187	.214	.238	.266	.285
12	.296	.338	.375	.419	.449	32	.184	.211	.234	.262	.281
13	.285	.325	.361	.404	.432	33	.182	.208	.231	.258	.277
14	.275	.314	.349	.390	.418	34	.179	.205	.227	.254	.273
15	.266	.304	.338	.377	.404	35	.177	.202	.224	.251	.269
16	.258	.295	.327	.366	.392	36	.174	.199	.221	.247	.265
17	.250	.286	.318	.355	.381	37	.172	.196	.218	.244	.262
18	.244	.279	.309	.346	.371	38	.170	.194	.215	.241	.258
19	.237	.271	.301	.337	.361	39	.168	.191	.213	.238	.255
20	.232	.265	.294	.329	.352	40	.165	.189	.210	.235	.252
				Appro	ximation		1.07	1.22	1.36	1.52	1.63
				For n	> 40		$\sqrt{\mathbf{n}}$	$\sqrt{\mathbf{n}}$	\sqrt{n}	$\sqrt{\mathbf{n}}$	\sqrt{n}
C	A 1	- 1 1			70 11	C . 1'	11 1	144		C D	

Source. Adapted by permission from Table 1 of Leslie H. Miller. Table of Percentage points of Kolmogorov statistics, J. Am. Stat. Assoc. 51 (1956). 111-121.

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SPACE FOR ROUGH WORK

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